

Homework Review
12) p 205 Quad Function
zeros 1 and -3
passes through (2, 10)
Write in Vertex Form

1) Factored $f(x) = a(x-1)(x-(-3))$
 $10 = a(2-1)(2+3)$
 $10 = a(1)(5)$
 $10 = 5a$
 $a = 2$

2) Factored $f(x) = a(x-1)(x-(-3))$
 $f(x) = 2(x-1)(x+3)$
 $\frac{s+t}{2} = \frac{-1+3}{2} = \frac{2}{2} = 1$
 $f(x) = 2(x-1)^2 + k$
 $f(1) = 2(-1)(+3) = -6$
 $f(1) = -6$
 $(h, k) = (1, -6)$
 $f(x) = a(x-h)^2 + k$
 $f(x) = 2(x-1)^2 - 6$
 $y = a(x-h)^2 + k$

Oct 20-9:32 AM

Functions 3 Forms

1) Standard $ax^2 + bx + c = 0$
 2) Vertex $f(x) = a(x-h)^2 + k$
 3) Factored $f(x) = a(x-s)(x-t)$

Standard to Vertex Form

Completing the Square

Mar 26-12:34 PM

$(a+b)^2 = a^2 + 2ab + b^2$
 $(a+b)(a+b)$ last term is a perfect \square
 middle term is $2ab$

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$(x+9)^2 \Rightarrow x^2 + 18x + 81$
 $(x-3)^2 \Rightarrow x^2 - 6x + 9$
 $(2x+5)^2 \Rightarrow 4x^2 + 20x + 25$
 $(x+4)^2 \Rightarrow x^2 + 8x + 16$
 $(3x-6)^2 \Rightarrow 9x^2 - 36x + 36$

Mar 26-12:46 PM

a) $f(x) = x^2 + 8x - 9$ $\left(\frac{b}{2}\right)^2$
 $f(x) = x^2 + 8x + 16 - 16 - 9$
 $f(x) = (x+4)^2 - 16 - 9$
 $f(x) = (x+4)^2 - 25$
 $(-4, -25)$ $a = +1$
 $h \quad k$

Make it
Square it
add it up
take it off

Mar 26-12:51 PM

$f(x) = x^2 - 6x - 14$ $\left(\frac{b}{2}\right)^2$
 $f(x) = x^2 - 6x + 9 - 9 - 14$ $(\frac{b}{2})^2 = 9$
 $f(x) = (x-3)^2 - 9 - 14$
 $f(x) = (x-3)^2 - 23$
 $(3, -23)$ $a = +1$
 $h \quad k$

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$f(x) = x^2 - 4x + 9$ $\frac{4}{2^2} = 4$
 $f(x) = x^2 - 4x + 4 - 4 + 9$
 $f(x) = (x-2)^2 - 4 + 9$
 $f(x) = (x-2)^2 + 5$
 $h \quad k$
 $(2, 5)$ $a = +1$

Oct 20-10:08 AM

$$\begin{aligned}
 f(x) &= 2x^2 + 20x + 5 \\
 f(x) &= 2(x^2 + 10x) + 5 && \text{Partial Factoring} \\
 f(x) &= 2(x^2 + 10x + 25 - 25) + 5 \\
 f(x) &= 2(x+5)^2 - 25 + 5 \\
 f(x) &= 2(x+5)^2 - 50 + 5 \\
 f(x) &= 2(x+5)^2 - 45 \\
 &\quad (-5, -45) \\
 &\quad \quad \quad h \quad k
 \end{aligned}$$

Mar 26-1:01 PM

$$\begin{aligned}
 &\text{Completing the Square} \\
 f(x) &= -x^2 + 6x + 7 \\
 &\text{Partial factor} \\
 f(x) &= -(x^2 - 6x) + 7 \\
 f(x) &= -(x^2 - 6x + 9 - 9) + 7 \\
 f(x) &= -[(x-3)^2 - 9] + 7 \\
 f(x) &= -(x-3)^2 + 9 + 7 \\
 f(x) &= -(x-3)^2 + 16
 \end{aligned}$$

Oct 10-10:43 AM

$$\begin{aligned}
 f(x) &= -3x^2 + 6x - 7 \\
 f(x) &= -3(x^2 - 2x) - 7 && \left(\frac{b}{2}\right)^2 \\
 f(x) &= -3(x^2 - 2x + 1 - 1) - 7 \\
 f(x) &= -3(x-1)^2 - 7 \\
 f(x) &= -3(x-1)^2 + 3 - 7 \\
 f(x) &= -3(x-1)^2 - 4 \\
 &\quad (1, -4)
 \end{aligned}$$

Mar 10-10:18 AM

$$\begin{aligned}
 f(x) &= -3x^2 + 15x - 2 \\
 f(x) &= -3(x^2 - 5x) - 2 \\
 f(x) &= -3\left[x^2 - 5x + \frac{25}{4} - \frac{25}{4}\right] - 2 && \left(\frac{5}{2}\right)^2 = \frac{25}{4} \\
 &\quad \quad \quad \frac{5}{2} \times \frac{5}{2} \\
 f(x) &= -3\left(x - \frac{5}{2}\right)^2 - \frac{25}{4} - 2 \\
 f(x) &= -3\left(x - \frac{5}{2}\right)^2 + \frac{75}{4} - 2 \\
 f(x) &= -3\left(x - \frac{5}{2}\right)^2 + \frac{75}{4} - \frac{8}{4} \\
 f(x) &= -3\left(x - \frac{5}{2}\right)^2 + \frac{67}{4} \\
 &\quad \left(\frac{5}{2}, \frac{67}{4}\right)
 \end{aligned}$$

Mar 26-1:07 PM

$$\begin{aligned}
 f(x) &= -2x^2 + 16x - 9 \\
 f(x) &= -2(x^2 - 8x) - 9 && \left(\frac{8}{2}\right)^2 \\
 &\quad \quad \quad (4)^2 \\
 f(x) &= -2(x^2 - 8x + 16 - 16) - 9 \\
 f(x) &= -2(x-4)^2 - 16 - 9 \\
 f(x) &= -2(x-4)^2 + 32 - 9 \\
 f(x) &= -2(x-4)^2 + 23 \\
 &\quad (4, 23)
 \end{aligned}$$

Oct 18-9:01 AM

$$\begin{aligned}
 f(x) &= -3x^2 + 24x - 12 \\
 f(x) &= -3(x^2 - 8x) - 12 \\
 f(x) &= -3(x^2 - 8x + 16 - 16) - 12 && \left(\frac{8}{2}\right)^2 = 16 \\
 f(x) &= -3(x-4)^2 - 16 - 12 \\
 f(x) &= -3(x-4)^2 + 48 - 12 \\
 f(x) &= -3(x-4)^2 + 36 \\
 &\quad (4, 36)
 \end{aligned}$$

Mar 26-1:09 PM

Hmk
P 214 q. 3, 4, 6 & 8

$$y = (x-3)^2 - 23$$

$(3, -23)$

$$y = a(x-h)^2 + k$$

(h, k)
 $(-4, -22)$

Mar 26-1:27 PM

$$f(x) = -x^2 - 6x - 14$$

$$f(x) = -1(x^2 + 6x) - 14$$

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Mar 10-10:46 AM